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## A robust ECG denoising technique using variable frequency complex demodulation

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## ABSTRACT

**Background and objective:** Electrocardiogram (ECG) is widely used for the detection and diagnosis of cardiac arrhythmias such as atrial fibrillation. Most of the computer-based automatic cardiac abnormality detection algorithms require accurate identification of ECG components such as QRS complexes in order to provide a reliable result. However, ECGs are often contaminated by noise and artifacts, especially if they are obtained using wearable sensors, therefore, identification of accurate QRS complexes often becomes challenging. Most of the existing denoising methods were validated using simulated noise added to a clean ECG signal and they did not consider authentically noisy ECG signals. Moreover, many of them are model-dependent and sampling-frequency dependent and require a large amount of computational time.

**Methods:** This paper presents a novel ECG denoising technique using the variable frequency complex demodulation (VFCDM) algorithm, which considers noises from a variety of sources. We used the sub-band decomposition of the noise-contaminated ECG signals using VFCDM to remove the noise components so that better-quality ECGs could be reconstructed. An adaptive automated masking is proposed in order to preserve the QRS complexes while removing the unnecessary noise components. Finally, the ECG was reconstructed using a dynamic reconstruction rule based on automatic identification of the severity of the noise contamination. The ECG signal quality was further improved by removing baseline drift and smoothing via adaptive mean filtering.

**Results:** Evaluation results on the standard MIT-BIH Arrhythmia database suggest that the proposed denoising technique provides superior denoising performance compared to studies in the literature. Moreover, the proposed method was validated using real-life noise sources collected from the noise stress test database (NSTDB) and data from an armband ECG device which contains significant muscle artifacts. Results from both the wearable armband ECG data and NSTDB data suggest that the proposed denoising method provides significantly better performance in terms of accurate QRS complex detection and signal to noise ratio (SNR) improvement when compared to some of the recent existing denoising algorithms.

**Conclusions:** The detailed qualitative and quantitative analysis demonstrated that the proposed denoising method has been robust in filtering varieties of noises present in the ECG. The QRS detection performance of the denoised armband ECG signals indicates that the proposed denoising method has the potential to increase the amount of usable armband ECG data, thus, the armband device with the proposed denoising method could be used for long term monitoring of atrial fibrillation.

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### 1. Introduction

The electrocardiogram (ECG) has been widely used for detection and classification of different life-threatening cardiac arrhythmias. For accurate detection of cardiac abnormalities, ECG signals must retain their morphological components in order to provide

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reliable and essential information about cardiac activity. However, ECGs are most often contaminated by a wide variety of noise sources including motion artifacts, bad electrode contact to the skin, and muscle and power line interference that can distort the ECG morphologies and lead to misdiagnosis of cardiac arrhythmias. Noise is more acute in ECGs from wearable devices simply because of movement artifacts. Therefore, it is very important and necessary to remove noise and artifacts from ECG signals in order to increase the usability of ECGs. However, denoising ECG signals is very challenging, especially if the noise frequency overlaps with the signal's frequency. There have been several denoising methods proposed in the literature in the last few decades. The most well-developed methods are based on discrete wavelet transform (DWT) decomposition [1–3], adaptive filtering [4, 5], empirical mode decomposition (EMD) and ensemble empirical mode decomposition (EEMD) [6–9], FIR filtering [10, 11], Kalman filtering [12], principal component analysis (PCA) [13], independent component analysis (ICA) [14], nonlocal means (NLM) [15], and neural networks [16, 17]. While many methods showed promising denoising performance, they have their own advantages and disadvantages.

The wavelet-based approaches [1–3] use soft and hard thresholding, which are popular for denoising non-stationary signals. However, wavelet-based methods cannot preserve the edges and are sensitive to intra-subject and inter-subject variations. Adaptive filtering approaches [4, 5] are often used for removing electromyogram (EMG) and motion artifacts. The main drawback of an adaptive filtering approach is that it requires a reference signal which is not often available.

The EMD-based approaches [6, 7] performed better when compared to wavelet-based thresholding methods, but they cannot completely remove noise. An adaptive switching mean filtering was proposed with EMD and DWT in [8] and a better result was shown when compared with previous EMD-based approaches. However, this approach needs an external QRS detector to preserve the QRS complexes. In addition, the EMD has a mode mixing problem [18]; as a result, the intrinsic mode functions (IMFs) extracted can be incorrect, decreasing the denoising performance.

The Kalman filtering approaches for denoising [12] are effective in preserving the edges of the signal. However, they require manual initialization of the parameters that are associated with the amplitude, width, and phase of the components of a complete ECG cycle. The PCA [13] and neural network [16] approaches require multiple leads to obtain better denoising performance using correlation. However, their performance is suboptimal for a single lead ECG. For ICA-based denoising [14], visual inspection of the independent components is essential, but this is not feasible for long-term applications. The non-local means (NLM) [15] method is a popular denoising technique that provides improvements in SNR. The main disadvantage of this approach is that its performance depends on the choice of a parameter's bandwidth, which depends on the noise standard deviation that might not be available in real time.

Some new ECG denoising techniques have been proposed in recent years such as the variational mode decomposition (VMD) method [19] and adaptive Fourier decomposition (AFD) [20]. An eigenvalue decomposition-based denoising is proposed in [21], where eigenvalue decomposition of the Hankel matrix approach is used for the baseline drift and powerline interference removal. A multi-lead model-based ECG signal denoising with an adaptive guided filter is proposed in [22]. Finally, convolutional encoder-decoder approaches were proposed in [17, 23]. However, the performance of these methods has not been compared with existing methods. Moreover, the deep learning-based approaches function as a black box, which requires more data for training and can be computationally expensive. Therefore, deep learning based denois-

ing may not be suitable in real time scenarios, especially for wearable device applications.

Most of the previously developed denoising methods were not validated using the realistic scenario of motion artifacts and muscle noise data; rather, they were tested on synthetically generated additive white Gaussian noise (AWGN) or random noise that were added to clean ECG signals.

In this paper, we propose a novel ECG denoising technique using the variable frequency complex demodulation (VFCDM) decomposition algorithm [24]. While a preliminary study of this method was published in the IEEE EMBC conference proceedings [25], this paper contains detailed results with a slight modification of parameters. We used the sub-band decomposition of a noisy ECG signal via the VFCDM to reconstruct a cleaner ECG signal by removing subcomponents that are associated with noise dynamics. Finally, we removed the baseline drift and abrupt noise components to achieve the final desired denoised signal. The performance of the proposed denoising technique was validated on the MIT-BIH arrhythmia database and the noisy ECG data obtained using a wearable armband device which was developed in the Chon lab [26]. We considered different types of noise sources both real and simulated to validate the proposed denoising technique. The simulated noises were used to compare the denoising performance with the existing denoising techniques since most of the denoising methods were validated using simulated noise. We used additive Gaussian white noise (AWGN), colored noise (blue, pink and violet), and powerline interference (PLI) to contaminate the ECGs and compared denoising performances of the proposed method with some of the existing denoising techniques. Moreover, the proposed method was tested using different real-life noisy conditions such as baseline wander, muscle noise, and electrode noises collected from the noise stress test database (NSTDB) [27]. Finally, the proposed method was successfully applied on the wearable armband ECG data corrupted by substantial amount of muscle artifact and the algorithm's performance was compared with some of the existing denoising techniques.

The rest of the paper is organized as follows: in the Materials and Methods section, we describe our dataset and present our proposed denoising algorithm. The performance of the proposed denoising technique is discussed in the Results section and perspective is provided in the Discussion section. Finally, a summary of the outcomes of our work is provided in the Conclusions section.

## 2. Materials and methods

### 2.1. Description of datasets

We considered ECG recordings from MIT-BIH arrhythmia database (MITDB), and our own wearable armband ECG database [26] to validate our proposed denoising technique. In addition, we collected the real noise sources from MIT-BIH noise stress test database (NSTDB) to contaminate the ECG records. The datasets are described below.

#### A) MIT BIH Arrhythmia Database

The MIT-BIH arrhythmia database is a well-known publicly available database. It consists of 48 half-hour long datasets of two-channel ambulatory ECG recordings which were obtained from 47 different subjects [27, 28]; 25 out of the 47 patients were male aged 32 to 89, and 22 were female aged 22 to 89. This database contains ECGs with a variety of waveforms and different abnormalities such as complex ventricular, junctional, and supraventricular arrhythmias and conduction abnormalities. The ECG recordings were digitized with a sampling frequency of 360 Hz and resolution of 11 bits over an 11mv range. Each recording consists of

two leads, one of which is modified limb lead II and the other was any of the following: V1, V2, V4, or V5.

#### A) Wearable Armband ECG Data

The armband ECG data were collected using a wearable armband device which has been developed in our lab at the University of Connecticut [26, 29]. This device has three pairs of hydrophobic electrodes, also developed in our lab [30], which are sequentially arranged for recording three different ECG channels. Because of the hydrophobic electrodes and the ease of wearability, this device is more comfortable than a typical Holter monitor that uses obtrusive leads and wet electrodes which are known to cause skin irritation. ECGs were obtained continuously for 24 hours with the armband worn on the upper left arm. The database contains 24 hours of continuous ECG recordings from each of the 16 healthy subjects aged  $27.56 \pm 8.82$  years (mean  $\pm$  standard deviation). The subjects were instructed to carry out their regular activities but without any intense exercise. In addition to the armband ECG, a simultaneous reference ECG was recorded with a very widely available Holter monitor (Rozinn RZ 153+, Glendale, NY, USA). All ECGs were obtained at a sampling frequency of 1000 Hz which were then down-sampled to 256 Hz.

#### A) The MIT-BIH Noise Stress Test Database

The MIT-BIH Noise Stress Test Database consists of 12 half hour ECG recordings and 3 half-hour recordings of noise in typical ambulatory ECG recordings [27, 28]. The noises include baseline wander, muscle artifact and electrode motion artifact which were made using physically active volunteers and standard ECG recorders, leads, and electrodes; the electrodes were placed on the limbs in positions in which subjects' ECGs were not visible. Calibrated amounts of different levels of noise were added to the two clean ECG recordings (118,119) from the MIT-BIH Arrhythmia Database. Different levels of noise were added to each of the recordings to make 6 different signals with different signal-to-noise ratios (SNRs) (24, 18, 12, 6, 0, and 6 dB). All the ECG signals were sampled with a sampling frequency of 360 samples per second.

### 2.2. VFCDM decomposition of noisy ECG signals

VFCDM is a high-resolution time-frequency analysis technique [24] that has been used for a variety of physiological signal processing [31–33]. While providing a high-resolution time-frequency spectrum (TFS), VFCDM also retains accurate amplitude distribution of the signal. Using VFCDM, we decomposed the noisy ECG into  $N_c$  ( $= 12$ ) number of modes or subbands.

$$Y_n(t) = \sum_{i=1}^{N_c} C_i(t) \quad (1)$$

In this equation,  $Y_n(t)$  is the noisy ECG signal,  $C_i$  represents the  $i_{th}$  frequency component, and  $N_c$  is the total number of subbands components (here,  $N_c = 12$ ). In this study, we decomposed the noisy ECG signal into 12 non-overlapping frequency bands using VFCDM. Given that the sampling frequency of the ECG was 360 Hz, the sub-band frequencies were equally spaced between 0 and 180 Hz.

### 2.3. Signal reconstruction

Fig. 1 shows an ECG segment of 2000 samples on which additive Gaussian white noise (AWGN) with a 20 dB signal-to-noise ratio level was superimposed, and its 12 VFCDM sub-band components. As can be seen from the figure, the frequency components after the 4th sub-band are noisy, with low amplitudes. It is also observable from Fig. 1 that most of the ECG components, especially

the P and T waves, are retained in the first component  $C_1$ . However, the QRS complex is attenuated and relatively wider than in the original ECG shown in Fig. Therefore, higher-frequency components (2–4) mostly contribute to the QRS complexes. We used only the first 4 components for our signal reconstruction.

To summarize again, the first component  $C_1$  preserves most of the ECG information and components 2 to 4 contribute to the morphology of the QRS complex. To reconstruct the de-noised signal, we compute an automated mask that preserves the values around only a small window of the QRS complex. We multiply components 2 to 4 by that mask to add them to the first component to obtain the final reconstructed signal. We start with reconstructing an intermediate signal,  $\tilde{Y}(t)$ , using the first two components. We perform a soft thresholding-based wavelet [2] denoising on the second component and added it to the first component to obtain an intermediate ECG signal,  $\tilde{Y}(t)$ .

$$\tilde{Y}(t) = C_1(t) + \widetilde{C_2}(t) \quad (2)$$

$\widetilde{C_2}(t)$  represents the wavelet-denoised  $C_2(t)$ . Next, we compute an automatic threshold using an approach similar to the one described in [34, 35]. A histogram is computed from the local maxima of  $\tilde{Y}(t)$ , from which the centroid is calculated using the following equation:

$$r = \frac{\sum_{i=1}^N x_i y_i}{\sum_{j=1}^N y_j} \quad (3)$$

where  $x_i$  is the signal magnitude,  $y_i$  is the distribution value of the signal, and  $r$  is the centroid of the histogram. Based on the centroid, we define a threshold,  $th = \alpha r$ , where  $\alpha$  is a multiplying factor (in this paper we used  $\alpha = 1$ ). Once the threshold is calculated, we determine all local maxima that satisfy the threshold criterion. As mentioned in [35], these local maxima correspond to the QRS complex peaks. The QRS complex peaks are then used to create a mask,  $m(t)$ , which is defined as follows:

$$m(t) = \begin{cases} \text{Tukey}(N, \gamma), & R(i) - \varepsilon \leq t \leq R(i) + \varepsilon \\ 0, & \text{else where} \end{cases} \quad (4)$$

where  $\text{Tukey}(N, \gamma)$  stands for a tapered Tukey window of length  $N$  ( $= 50$ ) with the tapering parameter  $\gamma$ ,  $R(i)$  represents the  $i_{th}$  QRS complex position,  $i$  varies from 1 to the total number of QRS complexes ( $N_R$ ), and the  $\varepsilon$  determines the spread of the Tukey window from the R peak. Depending on the noise level, the 2nd component  $C_2(t)$  of VFCDM can be either noisy or clean. In the case of a less-noisy ECG signal,  $C_2(t)$  will also be mildly affected by noise, hence, we want to use the entire  $C_2(t)$ . On the other hand, for a noisy ECG signal,  $C_2(t)$  is also noisy, consequently, we want to use only the QRS contribution to  $C_2(t)$ . In order to resolve this issue of using either the entire component or only the QRS part of  $C_2(t)$ , we define a power ratio  $P_r$  as follows:

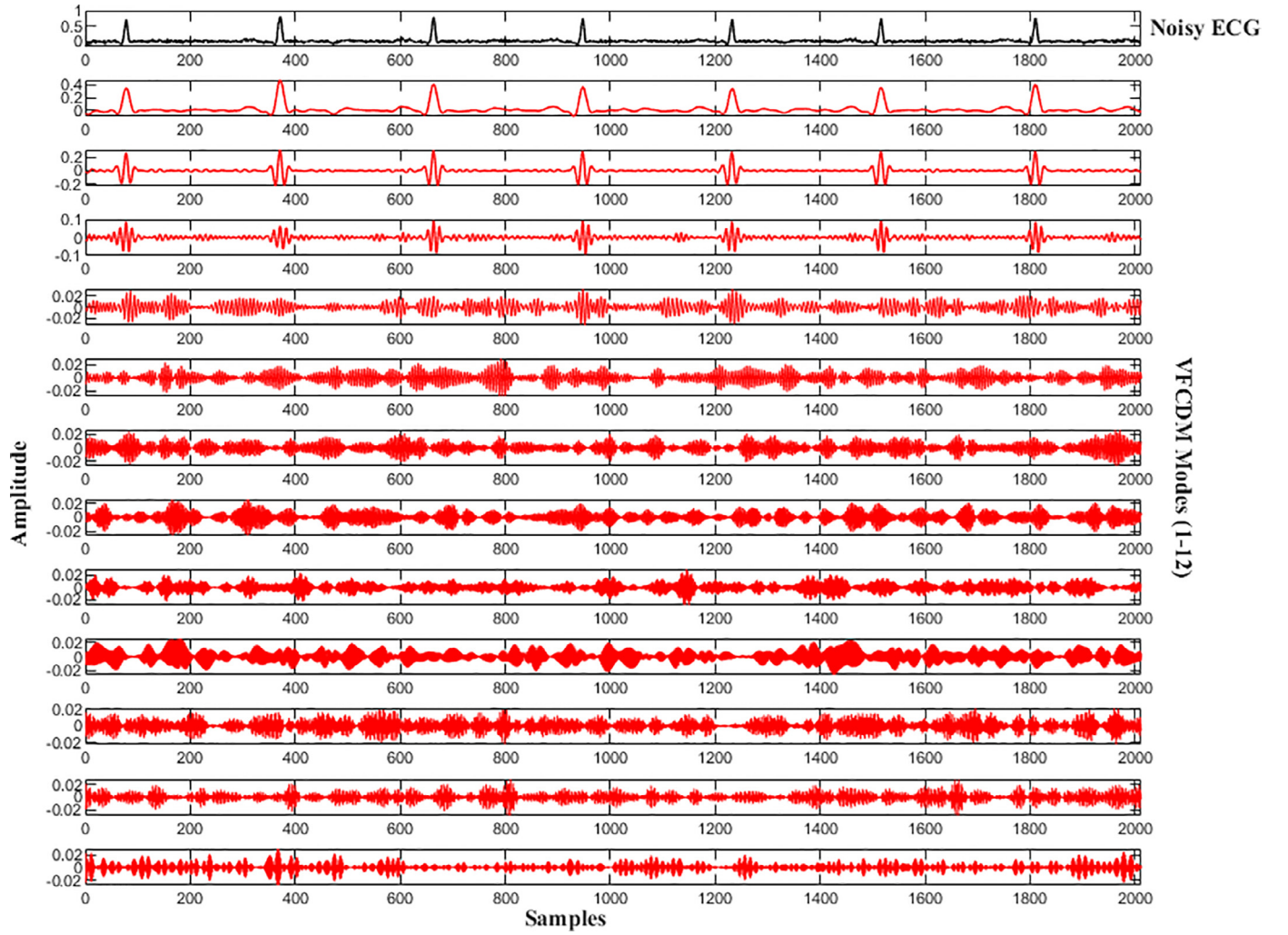
$$P_r = \frac{\text{Power of}(C_2(t) \times m(t))}{\text{Power of}(C_2(t))} \quad (5)$$

Based on the power ratio we use the following scheme for reconstruction of the signal:

$$Y_r(t) = \begin{cases} C_1(t) + \sum_{i=2}^4 C_i(t) \times m(t), & P_r < 0.9 \\ C_1(t) + C_2(t) + \sum_{i=3}^4 C_i(t) \times m(t), & P_r > 0.9 \end{cases} \quad (6)$$

A higher power ratio means most of the power of  $C_2(t)$  is concentrated around the QRS complex, so we use the entire  $C_2(t)$  in the reconstruction. On the other hand, a lower power ratio implies that  $C_2(t)$  has a substantial amount of power in the masked region, which is the case when  $C_2(t)$  is noisy. Therefore, we use masked





**Fig. 1.** VFCDM decomposition of a noisy ECG segment: a noisy ECG signal with a 20 dB SNR (record 106m from MITDB) (black line), VFCDM subcomponents: 1 to 12 (red lines).

$C_2(t)$  when the power ratio is low. Figure 2 shows the denoising steps performed, where the mask itself ( $m(t)$  in panel d) and the masked VFCDM components (in the panels e-g) are plotted in red to make them more distinguishable.

### 3. Results

The performance of the proposed denoising method was validated on the MIT-BIH arrhythmia database and the wearable armband ECG data obtained in our laboratory [26]. The performance of our proposed denoising technique on the MIT database will be compared with three other existing methods, namely NLM [15], wavelet soft thresholding [2], and EMD ASMF [8]. We define three performance metrics: SNR improvement ( $SNR_{imp}$ ), percentage root mean square difference (PRD), and mean square error (MSE), as these have been used as to evaluate other algorithms' performance [6, 8, 15]. The performance parameters are defined as follows:

$$SNR_{imp} = 10 \log_{10} \frac{\sum_{n=1}^N (Y_n[n] - Y[n])^2}{\sum_{n=1}^N (Y_d[n] - Y[n])^2} \quad (7)$$

$$PRD = \sqrt{\frac{\sum_{n=1}^N (Y_d[n] - Y[n])^2}{\sum_{n=1}^N Y^2[n]}} \times 100 \quad (8)$$

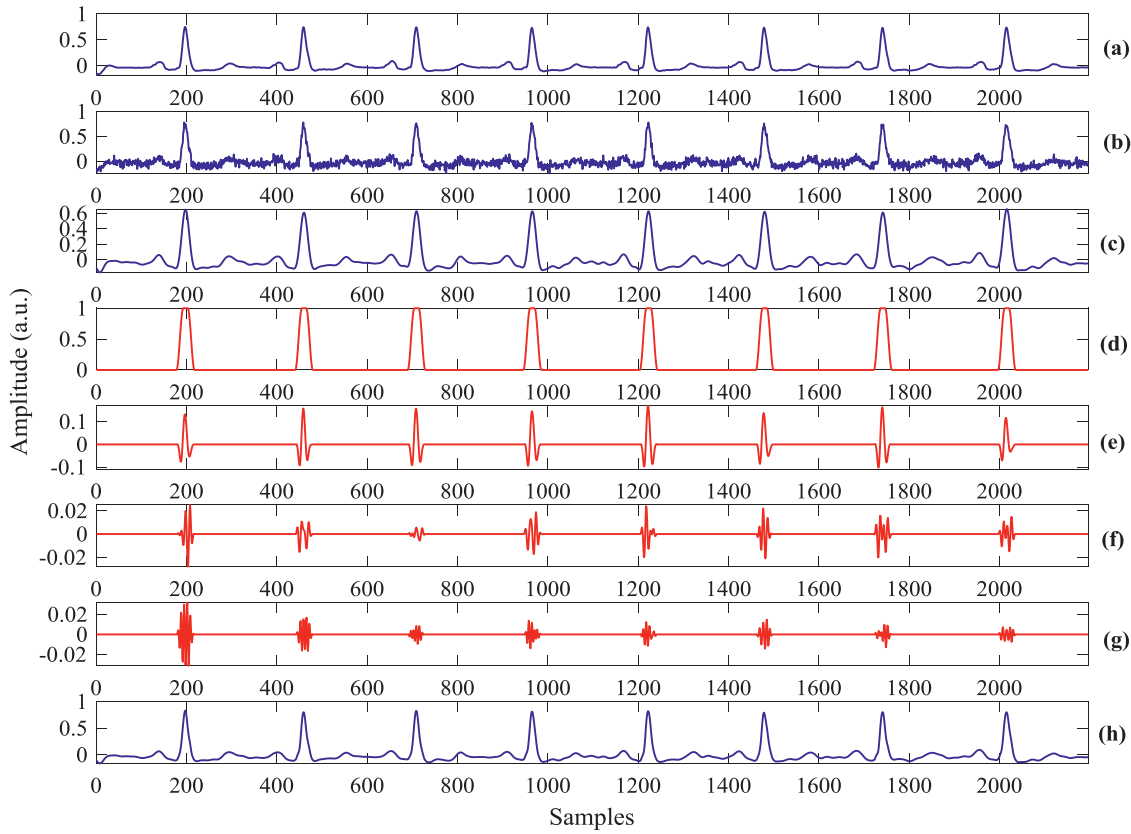
$$MSE = \frac{1}{N} \sum_{n=1}^N (Y_d[n] - Y[n])^2 \quad (9)$$

where  $Y_n[n]$  denotes noisy ECG,  $Y[n]$  stands for the original ECG,  $Y_d[n]$  represents the denoised ECG, and  $N$  is the length of the ECG signal. However, these performance metrics cannot be used to evaluate the denoising performance on the armband ECG data since we did not add noise by ourselves, rather, the armband's ECG contains the subject's muscle artifacts.

#### 3.1. Results on MIT-BIH arrhythmia database

In order to conform with most of the existing denoising methods [6, 8, 15], we considered ECG recordings 100m, 101m, 103m, 105m, 106m, 115m, 215m, and 230m from the MIT database for denoising performance comparison. We simulated different noise sources such as Gaussian white noise, powerline interference, and different colored noises (pink, blue, violet, and red) at 5 different SNR levels (-5 decibels (dB), 0 dB, 5 dB, 10 dB, 15 dB, and 20 dB). The powerline noise was simulated by producing a sinusoidal signal of 50 Hz using the approach described in [1] and the colored noise was generated using the method presented in [36].

#### A) Qualitative Analysis



**Fig. 2.** Denoising steps: (a) original ECG (subject 105) (b) ECG with AWGN noise at 10 dB SNR (c) first component of VFCDM decomposition (d) mask ( $m(t)$ ) (e-g) masked VFCDM components 2 to 4 (h) final reconstructed signal

We evaluate the quality of the denoised signal. Fig. 3 shows the denoised ECG signal using different methods on record 101m corrupted with blue noise at 0 dB SNR. Panel (f) of this figure reveals that the proposed denoising method provides discernible ECG waveforms while preserving ECG morphologies (i.e. P wave, T wave, and QRS complex) even at a low SNR. Note that in some cases, P and T waves can be of low amplitude. Even in those cases, the low-amplitude waves can be recovered, albeit this depends on the original state of the ECG morphology. A second denoising example is shown in Fig. 4. The ECG record 103m was corrupted with power line noise at -5 dB SNR. It can be observed that even at a very low SNR, the proposed method is able to obtain a relatively noise-free ECG segment while the EMD-ASMF method [8] shown in the panel (c) is unable to remove noise, and it distorts the QRS complexes at several time points.

In addition to adding synthetic noise, we also evaluated the proposed method with often-encountered noise artifacts such as baseline wander, muscle noise, and electrode noise, which are all found in the NSTDB. As can be seen from Fig. 5, the proposed method can effectively remove the baseline drift and muscle artifacts even at very low SNR (i.e. -5 dB). The performance of the method even on electrode noise is also reasonably good, given that electrode noise is considered to be one of the most difficult to remove.

The efficacy of the proposed method on ECG segments with arrhythmia is also visible from Fig. 5, which shows premature ventricular contraction (PVC) with bigeminy and trigemini patterns, and atrial flutter/fibrillation. All ECG records with these arrhythmias were corrupted by AWGN at 0 dB SNR and then the proposed denoising was applied.

As shown in Fig. 5, in each case the denoised and original ECG (prior to AWGN contamination) nearly overlap, which illustrates

that the proposed denoising technique is also effective even for ECGs with arrhythmias.

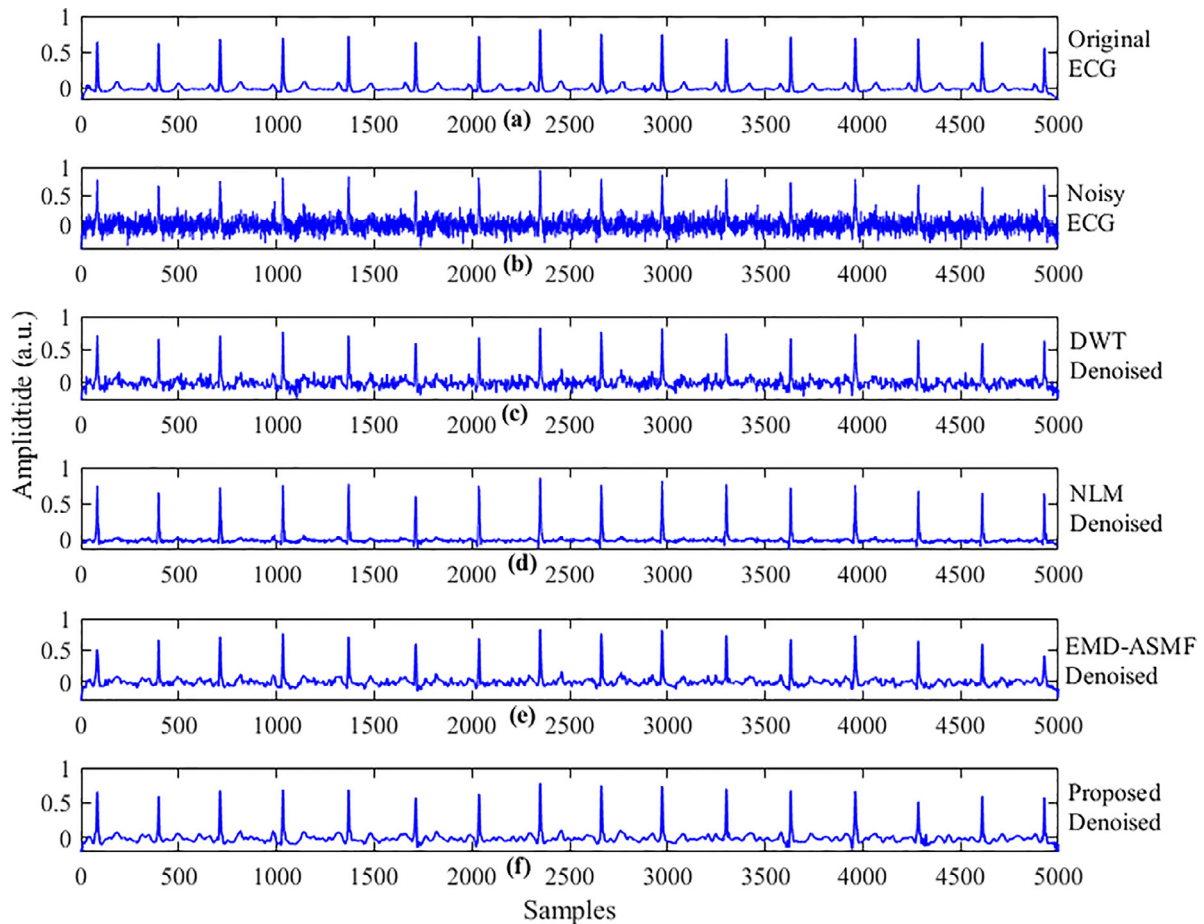
#### A) Quantitative Analysis

For quantitative analysis, we used the performance metrics defined in Eqs. (7)–(9). At a particular SNR level, a better denoising method is expected to provide higher  $SNR_{imp}$ , and lower PRD and MSE.

Fig. 6 shows the  $SNR_{imp}$  for all methods, at different SNR levels of added GWN, for the ECG records considered. It can be observed that the proposed denoising technique provided better  $SNR_{imp}$  at almost all SNR levels. Figs. 7 and 8 present a comparison of PRD and MSE results, respectively, for different denoising methods when GWN was added. These plots indicate that the proposed denoising method provides lower PRD and MSE than do the other methods considered.

As mentioned earlier, the proposed method performed well in removing power line interference. This is also visible from the performance metrics as well. Figs. 9 and 10 show  $SNR_{imp}$  and PRD results, respectively, using different denoising methods at different levels of power line noise. These figures show that the proposed denoising method has significantly higher  $SNR_{imp}$  and lower PRD when compared with the other denoising techniques. Fig. 11 shows a comparison of MSE results using different denoising methods for different levels of power line noise. It should be noted that the figure compares only two methods (the proposed and EMD-ASMF). The other methods were not used because of their high MSE values.

Finally, we considered three different colored noise scenarios, namely blue, pink, and violet to contaminate the ECG signals at different SNR levels and evaluated the denoising performance of the all methods considered. The detailed results are



**Fig. 3.** Blue noise removal in ECG: (a) original signal (record 101m from MIT database) (b) ECG with blue noise added at 0 dB SNR, and denoised ECG using (c) wavelet soft thresholding (d) NLM (e) EMD-ASMF (f) proposed method

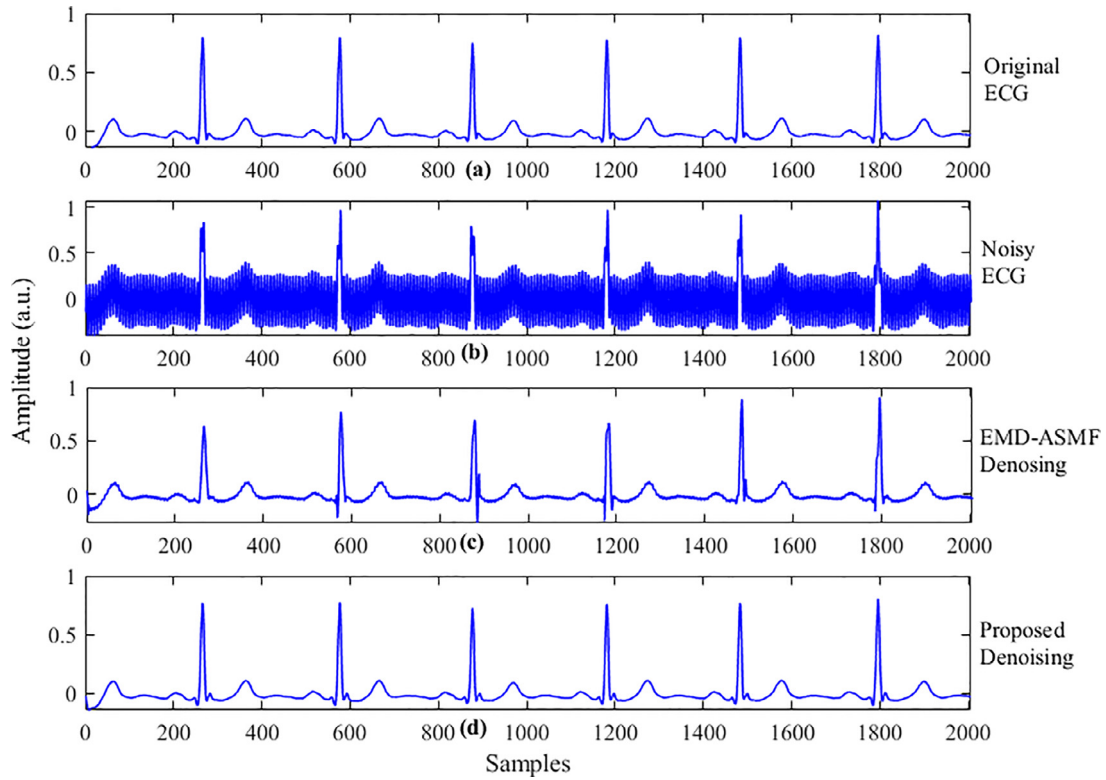
**Table 1**  
SNR improvement using three different types of additive colored noise

Methods	SNR in DB					
	Blue Noise					
	20	15	10	5	0	-5
Proposed work	5.0944	9.3574	12.7024	14.8720	16.4165	18.4695
EMD-ASMF	2.3103	6.7723	10.9340	14.2621	16.3226	17.2903
NLM	4.6744	5.8900	6.8032	7.8960	9.3034	10.3026
DWT	2.1952	5.0942	7.5028	9.6625	11.8605	14.2818
	Pink Noise					
Proposed work	0.4829	0.9825	3.4747	5.2371	6.4866	7.6391
EMD-ASMF	-1.0678	0.4826	1.1685	1.4352	1.5253	1.5213
NLM	1.5708	2.1777	2.9078	3.6712	4.2021	4.1623
DWT	-1.6188	-0.5260	0.1608	0.6376	0.9905	1.2164
	Violet Noise					
Proposed work	5.4434	10.2839	14.8359	18.7309	21.5255	23.2784
EMD-ASMF	2.4810	7.1487	11.8377	16.3480	20.1929	22.8851
NLM	4.4247	5.5835	6.4479	7.4529	8.7023	9.5548
DWT	3.5503	7.1352	10.2412	12.8445	15.1321	17.6662

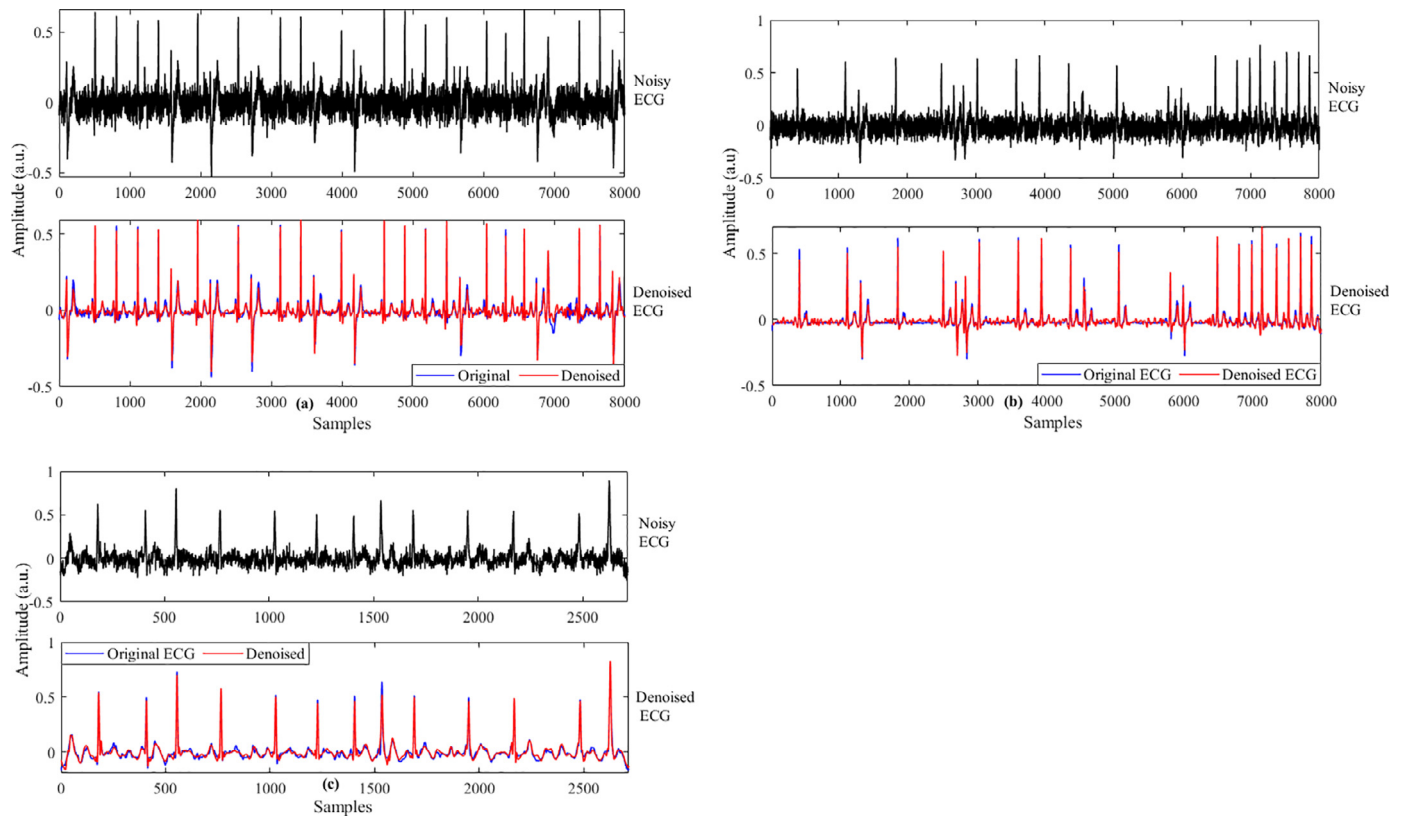
shown in Tables 1, 2, and 3, respectively. Table 1 presents the  $SNR_{imp}$  for all the denoising techniques, at different levels of colored noise. It can be observed from Table 1 that for blue and violet noise, most of the denoising techniques performed well and provided higher  $SNR_{imp}$ . The proposed method has the highest SNR improvement at almost all SNR levels. In the case of pink noise, most of the methods failed to provide good denoising performance, which can be observed from the  $SNR_{imp}$  values. The table shows that even in the case of pink noise, the proposed method provided reasonably higher  $SNR_{imp}$ . The same conclusion

can be drawn from Tables 2 and 3, which show the PRD and MSE values, respectively. The proposed method provided significantly lower PRD and MSE values when compared with the other existing techniques.

In addition to  $SNR_{imp}$ , PRD, and MSE as performance metrics, we have also used the wavelet energy diagnostic distortions (WEDD) metric, as proposed in [37]. WEDD is a standard and popular diagnostic distortion measure that has been used previously in a recent ECG denoising literature [38]. The lower the WEDD, the better the denoising performance. According to the criteria given in [37], the



**Fig. 4.** Power line interference removal: (a) original signal (record 103 from MITDB) (b) ECG with added PLI at -5 dB SNR (c) denoised ECG using EMD-ASMF (d) denoised ECG using the proposed method

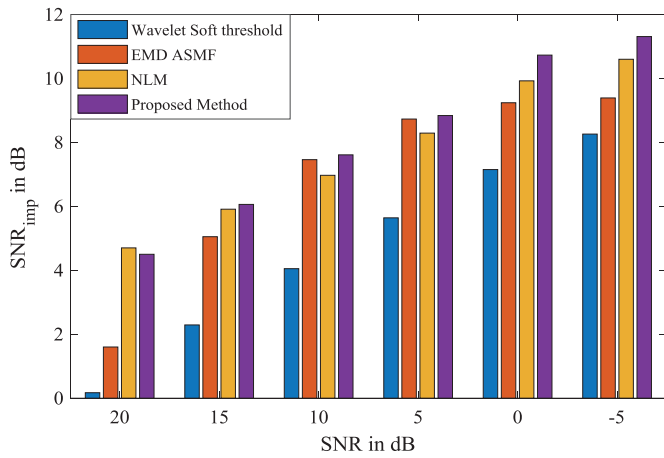


**Fig. 5.** Proposed denoising applied on arrhythmic ECGs: (a) PVCs with bigeminy (record 106 from MITDB) (b) PVC with ventricular trigeminy (record 201 from MITDB) (c) Atrial Flutter/fibrillation (record 222 from MITDB)

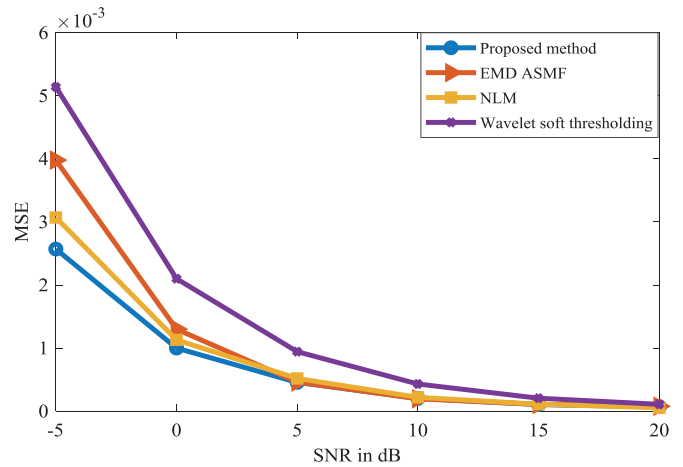


**Table 2**  
PRD using three different types of additive colored noise

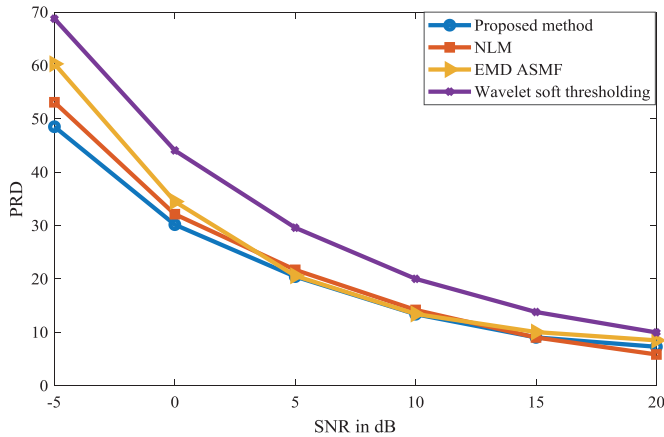
Methods	SNR in dB					
	Blue noise					
	20	15	10	5	0	-5
Proposed work	6.3162	6.6447	7.6078	10.0169	15.2195	20.9380
EMD-ASMF	7.8622	8.3507	9.1443	10.9798	15.3075	24.3119
NLM	6.1321	9.0661	14.4856	22.7010	34.4293	55.1862
DWT	8.0125	10.0851	13.5351	18.8132	25.9923	34.8458
	Pink Noise					
Proposed work	10.8961	16.3299	21.4156	30.6806	47.5306	74.1099
EMD-ASMF	11.8464	17.2420	27.6528	47.9171	84.0416	149.2678
NLM	9.3620	14.2122	22.6752	36.9512	61.8522	110.3761
DWT	12.1424	18.9401	31.0743	52.2812	89.2512	154.6188
	Violet Noise					
Proposed work	6.1790	6.2344	6.4198	6.9632	8.4366	11.8962
EMD-ASMF	7.7177	8.0254	8.3177	8.7559	9.9083	12.8178
NLM	6.0433	9.3884	15.0879	23.8854	36.8617	59.9528
DWT	6.9331	8.0521	9.9215	13.0995	17.8841	23.9432



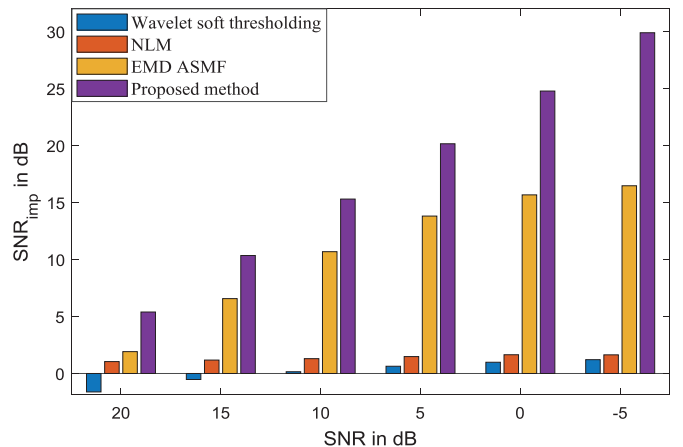
**Fig. 6.** Comparison of  $SNR_{imp}$  for different denoising methods with Gaussian white noise contamination.



**Fig. 8.** Comparison of  $MSE$  for different denoising methods with Gaussian white noise.



**Fig. 7.** Comparison of  $PRD$  for different denoising methods with Gaussian white noise contamination.



**Fig. 9.** Comparison of  $SNR_{imp}$  with different denoising methods for removal of power line interference.

denoising performance can be ranked as (1) excellent ( $WEDD < 4.517\%$ ), (2) very good ( $WEDD$  is within  $4.517\% - 6.914\%$ ), (3) good ( $WEDD$  is within  $6.914\% - 11.125\%$ ), (4) not bad ( $WEDD$  is within  $11.125\% - 13.56\%$ ), (5) Bad ( $WEDD > 13.56\%$ ).

Table 4 shows the denoising performance comparison in terms of  $WEDD$  at different levels of SNR. It can be seen from the table that the proposed VFCDM-based denoising results in smaller

$WEDD$  in most of the SNR cases (especially at higher SNR). At 20 dB, the NLM has slightly lower  $WEDD$  than the proposed denoising method. However, this smaller  $WEDD$  is insignificant since the signal at 20 dB is not considered to be noisy. The proposed denoising method was able to remove the power line interference noise even at a very low SNR level (e.g.  $< 0$  dB). In terms of  $WEDD$ , the pro-



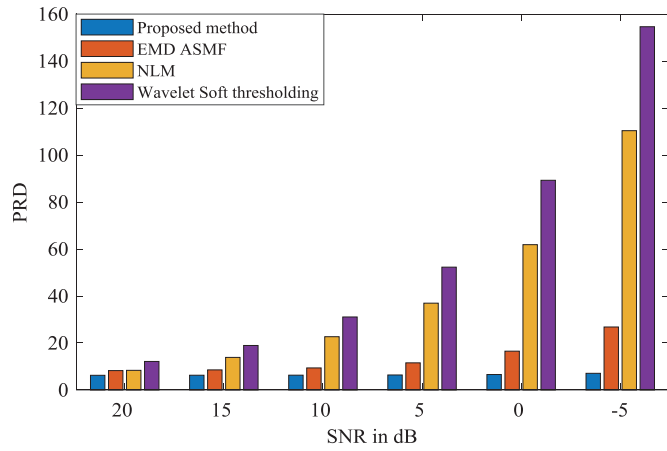


Fig. 10. Comparison of PRD with different denoising methods for removal of power line interference.

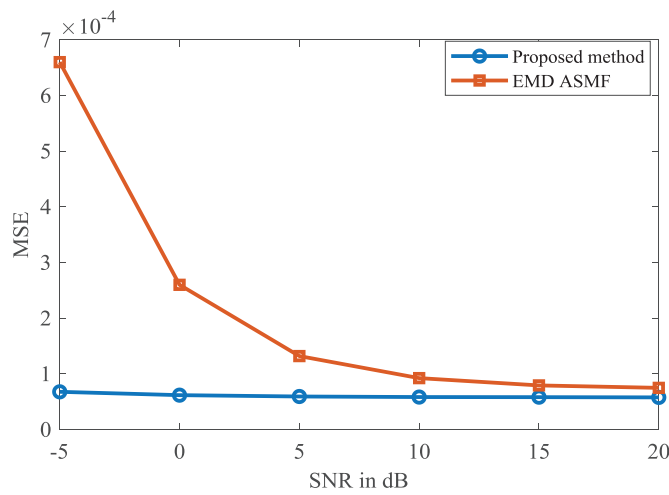


Fig. 11. Comparison of MSE of different denoising methods for power line interference.

Table 3 MSE ( $\times 10^{-3}$ ) on three different additive colored noise types

Methods	SNR in dB					
	20	15	10	5	0	-5
Blue Noise						
Proposed work	0.058	0.063	0.079	0.130	0.259	0.508
EMD-ASMF	0.067	0.075	0.089	0.129	0.253	0.643
NLM	0.047	0.089	0.227	0.566	1.290	3.310
DWT	0.071	0.110	0.197	0.381	0.731	1.310
Pink Noise						
Proposed work	0.137	0.291	0.497	1.040	2.460	5.880
EMD-ASMF	0.139	0.307	0.834	2.490	7.720	24.500
NLM	0.095	0.278	0.566	1.500	4.200	13.400
DWT	0.16	0.389	1.050	2.980	8.700	26.200
Violet Noise						
Proposed work	0.054	0.057	0.060	0.068	0.096	0.177
EMD-ASMF	0.064	0.069	0.075	0.083	0.105	0.176
NLM	0.040	0.095	0.247	0.626	1.480	3.900
DWT	0.055	0.072	0.107	0.185	0.344	0.623

posed denoising method performs excellently at 20 dB, very good at 15 dB, 10dB, 5 dB, and 0 dB, and good at -5 dB, according to the defined criteria [37].

Finally, we analyzed the performance of the proposed denoising method on MIT-BIH's NSTDB. This database contains three different types of noise sources commonly encountered in practice, namely,

Table 4 Diagnostic distortion comparison (WEDD)

Methods	SNR in dB					
	AWGN					
	20	15	10	5	0	-5
Proposed work	5.01%	6.79%	11.01%	15.28%	22.41%	43.21%
EMD-ASMF	6.87%	8.63%	12.34%	19.64%	33.27%	58.51%
NLM	4.68%	6.90%	11.21%	17.27%	25.74%	47.99%
DWT	8.51%	10.79%	18.08%	24.58%	38.79%	59.68%
Power line interference (PLI)						
Proposed work	4.13%	5.76%	5.78%	5.90%	6.28%	7.31%
EMD-ASMF	5.85%	6.00%	6.44%	7.57%	10.17%	15.57%

Table 5 Performance on NSTDB

Parameter	SNR in dB					
	Baseline wander					
	20	15	10	5	0	-5
SNR <sub>imp</sub>	3.8918	7.8178	12.4083	16.5442	20.0098	22.44
PRD	5.04%	6.77%	7.58%	8.37%	9.99%	11.43%
WEDD	4.81%	5.01%	6.31%	6.83%	7.13%	9.05%
Muscle Noise						
SNR <sub>imp</sub>	4.1701	7.5015	9.7676	10.8946	12.5031	13.9935
PRD	5.79%	7.44%	10.93%	15.71%	23.82%	41.05%
WEDD	4.82%	6.52%	8.94%	13.72%	20.32%	35.67%
Electrode Noise						
SNR <sub>imp</sub>	3.8092	6.9039	7.8119	8.8452	9.3541	9.9778
PRD	7.01%	9.81%	12.01%	21.09%	32.57%	56.91%
WEDD	5.36%	8.61%	11.07%	19.85%	29.71%	48.67%

baseline wander (BW), muscle noise (MN), and electrode motion artefact (EM) [27]. We added these three noise sources at 6 different SNR levels to the ECG records from the MITDB. The performance of the proposed denoising method was evaluated in terms of both non-diagnostic distortion ( $SNR_{imp}$ , PRD) and diagnostic distortion (WEDD). The proposed method's performance is shown in Table 5. As shown, the proposed method was able to remove the baseline wander even at very low SNR, providing higher  $SNR_{imp}$ , and lower PRD and WEDD values. The worst WEDD is 9.05% (at -5 dB) which still falls in the "good" range (6.914% - 11.125%). The proposed denoising method showed promising results in removing muscle noise as well. It should be noted that many of the previous studies [8, 39] simulated muscle noise using random noise generation, however, in this study, we used true muscle noise data. Removing electrode noise is considered the most troublesome since it can mimic the appearance of ectopic beats and the noise frequency components' dynamics significantly overlap with the ECG components [10]. The proposed denoising technique performed satisfactorily in removing electrode noise, as also shown in Table 5.

The overall results suggest that the proposed method has superior denoising performance in almost all noisy conditions. The NLM [15] method is quite effective in removing GWN but it does not work well on other noise types such as PLI and colored noise. On the other hand, the EMD-ASMF [8] works well in removing power line noise, but its performance is poor with pink noise. DWT-based denoising [2] could not fully remove the noise when the ECG signal was highly corrupted. Note that all of these compared methods performed poorly on NSTDB noise, which is why their results were not included in Table 5.

### 3.2. Results on the armband ECG data

In order to evaluate the performance of the proposed denoising technique on the armband ECG, we randomly chose 40 ten-second segments of both noisy and clean ECG channels from the arm-

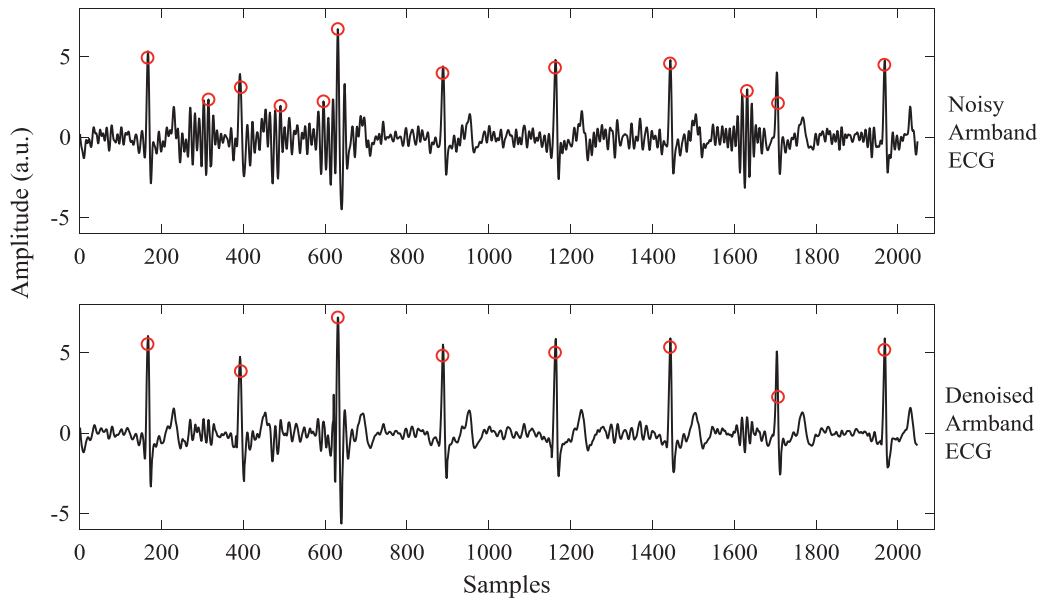


Fig. 12. QRS complex detection on (a) armband ECG segment with muscle artifact (b) the same segment, denoised.

Table 6

QRS detection performance comparison

Denoising Method	Correctly detected R peaks	$SNR_{imp}$ (mean $\pm$ sd)
DWT	79.4871%	0.0569 $\pm$ 0.0376
EMD-ASMF	92.8826%	1.0568 $\pm$ 0.6342
Proposed method	92.9577%	1.4595 $\pm$ 0.6326

band ECG database [26]. Adjudication of clean versus noisy ECG data was determined visually by three of the authors (N.R., K.H.C., and J.L.) based on the presence of P, Q, R, S, and T waves in the ECG segments. The denoising performance on the ECG segments was evaluated and compared in terms of accurate R peak detection and SNR improvement. For R peak detection, we used the Pan and Tompkins R-peak detection algorithm [40] on the denoised sequences. Detected R peaks were visually inspected by three independent experts and the majority vote was taken as the correct decision. SNR improvement was calculated by subtracting the noisy signal SNR from the denoised signal SNR, as described in [23].

QRS complex detection on the representative segments of noisy armband and denoised armband ECG signals is shown in Fig. 12. It can be observed that due to excessive EMG noise artifacts, there are several R peak misdetections and false positives in the noisy armband data (upper panel), which are avoided in the denoised armband ECG (bottom panel). The summary of the denoising performance and comparison on the armband ECG data is provided in Table 6. As we can see from the table, the proposed denoising method provides the highest percentage (92.9577%) of correctly detected R peaks. EMD-ASMF provides nearly the same percentage of correctly detected R peaks. However, this method requires an external QRS complex detector in order to preserve them in the process of denoising, and hence, the performance of EMD-ASMF is quite dependent on QRS complex detection algorithm. Table 6 also shows that the proposed denoising method provides significantly higher SNR improvement (1.4595) when compared to that of the DWT and EMD-ASMF denoising methods. As stated earlier, the NLM has a parameter bandwidth which is dependent on the noise standard deviation, which is unknown in the noisy ECG data. Therefore, we could not compare the proposed denoising method with NLM for the armband ECG data.

#### 4. Discussion

The results presented in this paper demonstrate that the proposed denoising method provided better denoising performance when compared to other denoising techniques in a variety of noise-corrupted scenarios. We showed that the VFCDM-based sub-band decomposition of noisy ECG signals was more effective than EMD or wavelet-based denoising techniques in separating noisy components from the clean ECG. The proposed denoising method provided cleaner ECG segments and also retained ECG morphologies (i.e. P wave, T wave, and QRS complexes).

We considered ECG signals corrupted with different types of noise at different levels of SNR to evaluate the denoising performance on a variety of noisy conditions. The results in this paper indicate that most of the existing methods considered in this paper did not perform adequately in removing noise from a wide range of sources. For example, NLM [15] provided good denoising performance in AWGN noise but its performance on removing PLI and colored noise was found to be poor. The EMD-ASMF [8] technique provided poor denoising performance on ECG signals corrupted with pink colored noise while the wavelet soft thresholding method [2] could not remove noise entirely in most of the cases.

The qualitative and quantitative analysis of the denoising results indicate that the proposed denoising technique can provide better-quality denoised ECG with higher  $SNR_{imp}$  as well as lower PRD and MSE values than the existing denoising techniques considered. In ECGs contaminated with AWGN, the proposed denoising method provided higher  $SNR_{imp}$  and lower PRD and MSE at almost all SNR levels than NLM, EMD-ASMF and DWT-based techniques. At 20 dB SNR, the SNR improvement using the NLM method [15] was slightly higher than our proposed method, however, this improvement was not significant because it had negligible effect on the ECG quality. The same was true for PRD and MSE as well.

The denoising performance of our proposed method on the PLI-corrupted ECG signals was found to be better than any of the methods compared. The sub-band decomposition of the noisy signals enabled the noise-free reconstruction of the ECG at a low SNR level. The  $SNR_{imp}$  resulting from the proposed denoising method was significantly larger than that of the existing methods. Moreover, the PRD and MSE values were almost constant across differ-

ent levels of SNR, which indicates that the proposed method can remove PLI noise almost equally good at different levels of SNR. Even though the EMD-ASMF method can remove PLI to a great extent, this method failed to retain the QRS amplitudes, especially at lower input SNR levels. Moreover, it was not able to remove noise components, especially at low SNR levels.

Similar to the AWGN and PLI cases, the proposed method also showed superior denoising performance on ECGs corrupted with colored noise, when compared to the existing denoising techniques. While the other methods showed low  $SNR_{imp}$  and higher PRD and MSE values for the ECGs contaminated with pink noise at low input SNR levels, in this case the proposed method provided sufficient  $SNR_{imp}$ , and reasonable PRD and MSE values.

The major advantage of the proposed method is that it has been tested using different noise sources that are often observed in practice, such as baseline wander, muscle noise, and electrode noise, whereas most of the existing denoising methods were evaluated using synthetic noise. The proposed method was shown to remove baseline wander even at very low SNR levels without any significant distortion of the ECG morphologies (WEDD is a maximum of 9.05% at -5 dB SNR). Sufficiently good results were obtained in the case of muscle noise as well. Moreover, the application of the proposed denoising algorithm on the wearable armband ECG data which are contaminated with muscle artifacts showed significantly better performance when compared to the other methods considered in this study.

The proposed method showed a moderate performance in the case of electrode noise situations. This is because electrode noise can mimic the appearance of ectopic beats and the dynamics of the noise are highly overlapped with the ECG components. Thus, removing electrode noise is known to be difficult.

Finally, the application of the proposed denoising method on the noisy armband ECG data did improve the QRS complex detection accuracy. This result indicates that the proposed denoising method can significantly enhance the accuracy of R-R interval based cardiac arrhythmia (e.g. atrial fibrillation (AF) [41]) detection.

## 5. Conclusions

We presented a novel ECG denoising technique using a high time-frequency resolution method. The proposed method was validated on the standard MIT-BIH arrhythmia database with a variety of noise (i.e. AWGN, colored noise (blue, pink, and violet), PLI, baseline wander, electrode noise, and muscle artifacts) at different SNR levels, and its performance was compared with three other existing denoising methods. In most of the noisy scenarios, the proposed method showed better denoising performance over the other methods. The application on the arrhythmic ECGs suggest that the proposed denoising method is equally applicable for both regular and arrhythmic ECGs. Finally, the proposed method was successfully applied to the armband ECG signals and it was able to remove significant EMG artifacts, consequently providing more accurate R-peak detection. The QRS complex detection results on the denoised armband data demonstrate that the proposed denoising method could significantly enhance the potential of the armband device to be used for continuous monitoring of AF, and without the skin irritation that has been a problem for Holter monitors because of their hydrogel electrodes.

## Declaration of Competing Interest

The authors declare no conflicts of interest.

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